**PCA**

**Class Architicture:**

We have totally **7** function:

* **The constructor:**

We specify the number of the component (new features) that we want our data to have, and it specifies two variables, one to store the **component**, and another one to store the **mean**

* **Normalization:**

To standardize the data using the mean

* **Covariance:**

To calculate the covariance matrix

* **Calc\_eigen:**

To calculate the eigen values and vectors

* **Fit:**

It is the main function of our class

* **Transform:**

It takes the data matrix then transform it to the new **reduced data** using the same object after performing its **Fit function**

* **Reverse:**

Trying to de-transform the new (reduced) data to its original values

**Eigen:**

To calculate the Eigen Values and Vectors we made custom function using **sympy** library, the function has the following sub-functions:

* **calc\_determinant:**

its custom **recursive** function using **divide and conquer** method, to calculate the determinant of a given matrix by:

1. checking if the shape of a function is (2,2) if its true then the determinant is the:

(value [0][0] \* value [1][1]) – (value [0][1] \* value [1][0])

1. if the shape of the matrix is not a (2,2) then I will divide the matrix into **M** **sub-matrices**, which **M** is the number of **columns** or **rows** in the parent matrix “note the matrix is squared matrix so number of rows = number of columns”.

these new matrices will have the shape of (M-1, M-1) because we are removing the first row and **T’th column**, which **T** is the number of the **sub-matrix**.

We calculate the determinant to the sub-matrices using the same function, the final determinant to the original matrix will be:

the summation of all the sub-determinant each sub-determinant multiplied by (-1)^T and its **T** value “value [0][T] from the parent matrix” from the first row

see the following formula

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* calc\_eigenvalues:

its custom function takes the result of:

A black symbols of a mathematical equation

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Let’s make the above formula equals to matrix called Result, our calc\_eigen function takes the Result function then forming from it the equation of the determinant

then finding the values of Lambda that makes the determinant equals to zero by using Eq, and solve functions from sympy library

* calc\_eigenvectors:

in this function we are calculating the eigen vectors using the eigen values and Result matrix.

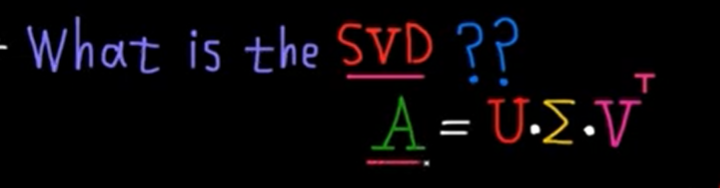
but we faced a problem:

**Problem Definition**

that the determinant of The Result matrix after substituting the Lambda with an Eigen value not always Equal to zero some-times the determinant is a very small value it almost equal to zero, that’s due to the Floating-point precision , and this make the solve functions from sympy library consider the matrix is not singular and give us trivial solution witch is all the vectors are equals to zeros, when in the same time its theoretically should equal to zero for the eigenvalues

**Attempt (1) using SVD Only as an attempt to solve Floating-point**

So we used **SVD** (Singular Value Decomposition) matrix analyzation its robust to numerical issues because it works with floating-point approximations and doesn't rely directly on symbolic solvers, because it’s can give us a singular matrix and its determinant is exactly equal to **zero**



We can choose U or V^T use V^T because there are both squared matrices, and their vectors are perpendicular on each other, we apply the SVD on our Result matrix then we, took a single vector from the V^T for its corresponding eigen value but we found another problem the dot product between the resulting eigen vectors its not equals to zero

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Its equal to very small number almost equal zero

Comparing to the built-in numpy array:A black screen with white text

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We found it’s having the same problem, and we found out that the complexity of the determinant function is O(n!)

**Attempt (2) using Power Iteration for Eigen…**